What is claimed is:

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A method of indexing a database of documents, comprising:

providing a vocabulary of n terms;

indexing the database in the form of a non-negative $n \times m$ index matrix V,

5 wherein:

m is equal to the number of documents in the database;

n is equal to the number of terms used to represent the database; and the value of each element v_{ij} of index matrix V is a function of the number of occurrences of the ith vocabulary term in the jth document;

factoring out non-negative matrix factors T and D such that

 $V \approx TD$; and

wherein T is an $n \times r$ term matrix, D is an $r \times m$ document matrix, and r < r

nm/(n+m)

- 2. The method of claim 1 further comprising deleting said index matrix V.
- 3. The method of claim 2 further comprising deleting said term matrix T.
- 4. The method of claim 1 wherein r is at least one order of magnitude smaller than n.

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- 5. The method of claim 1 wherein r is from two to three orders of magnitude smaller than n.
- 6. The method of claim 1 wherein entries of said document matrix D falling below a predetermined threshold value t are set to zero.
- 7. The method of claim 2 wherein r is at least one order of magnitude smaller than n.
- 8. The method of claim 2 wherein r is from two to three orders of magnitude smaller than n.
- 9. The method of claim 2 wherein entries of said document matrix D falling below a predetermined threshold value t are set to zero.
- 10. The method of claim 3 wherein r is at least one order of magnitude smaller than n.
- 11. The method of claim 3 wherein r is from two to three orders of magnitude smaller than n.
- 12. The method of claim 3 wherein entries of said document matrix D falling below a predetermined threshold value t are set to zero.

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The method of claim 1 wherein said factoring out of non-negative matrix (13. factors T and D further comprises:

selecting a cost function and associated update rules from the group:

cost function
$$F = \sum_{i=1}^{n} \sum_{j=1}^{m} [V_{ij} \log(TD)_{ij} - (TD)_{ij}]$$
 associated with

update rules
$$T_{ik} \leftarrow T_{ik} \sum_{j=1}^{N} \frac{V_{ij}}{(TD)_{ij}} D_{kj}$$
, $T_{ik} \leftarrow \frac{T_{ik}}{\sum_{l} T_{lk}}$, and $D_{kj} \leftarrow D_{kj} \sum_{i} T_{ij} \frac{V_{ij}}{(TD)_{ij}}$,
$$Cost function F = \sum_{i=1}^{n} \sum_{j=1}^{m} \left[V_{ij} \log \frac{V_{ij}}{(TD)_{ij}} - (V_{ij}) + (TD)_{ij} \right] \text{ associated with}$$

$$\sum_{i} \frac{T_{ik} V_{ij}}{(TD)_{ij}} \sum_{j=1}^{n} \left[V_{ij} \log \frac{V_{ij}}{(TD)_{ij}} - (V_{ij}) + (TD)_{ij} \right] \text{ associated with}$$

cost function
$$F = \sum_{i=1}^{n} \sum_{j=1}^{m} \left[V_{ij} \log \frac{V_{ij}}{(TD)_{ij}} - (V_{ij}) + (TD)_{ij} \right]$$
 associated with

$$\text{update rules } D_{kj} \leftarrow D_{kj} \frac{\displaystyle\sum_{i} \frac{T_{ik}V_{ij}}{(TD)_{ij}}}{\displaystyle\sum_{l} T_{lk}} \text{ and } T_{ik} \leftarrow T_{ik} \frac{\displaystyle\sum_{j} \frac{D_{kj}V_{ij}}{(TD)_{ij}}}{\displaystyle\sum_{h} D_{kh}} \text{ , and }$$

$$\text{cost function } \|V - TD\|^2 = \sum_{i=1}^n \sum_{j=1}^m (V_{ij} - (TD)_{ij})^2 \quad \text{associated with update}$$

$$\text{rules } D_{kj} \leftarrow D_{kj} \frac{(T^T V)_{kj}}{(T^T TD)_{kj}} \quad \text{and} \quad T_{ik} \leftarrow T_{ik} \frac{(VD^T)_{ik}}{(TDD^T)_{ik}}; \text{ and}$$

iteratively calculating said update rules so as to converge said cost function toward a limit until the distance between V and TD is reduced to or beyond a desired value.

14. A program storage device readable by machine, tangibly embodying a program of instructions executable by the machine to perform method steps for indexing a database of documents, said method steps comprising:

providing a vocabulary of n terms:

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indexing the database in the form of a non-negative $n \times m$ index matrix V,

wherein

m is equal to the number of documents in the database;

n is equal to the number of terms used to represent the database; and

the value of each element v_{ij} of index matrix V is a function of the number

of occurrences of the ith vocabulary term in the jth document;

factoring out non-negative matrix factors T and D such that

 $V \approx TD$; and

wherein T is an $n \times r$ term matrix, D is an $r \times m$ document matrix, and $r < \infty$

nm/(n+m).

15. A database index, comprising:

an $r \times m$ document matrix D, such that

 $V \approx TD$

wherein T is an $n \times r$ term matrix;

V is a non-negative $n \times m$ index matrix, wherein each of its m columns represents an jth document having n entries containing the value of a function of the number of occurrences of a ith term appearing in said jth document; and

wherein T and D are non-negative matrix factors of V and r < nm/(n+m);

and

wherein each of the m columns of said document matrix D corresponds to said jth document.

16. A method of information retrieval, comprising:

providing a query comprising a plurality of search terms;

providing a vocabulary of *n* terms;

performing a first pass retrieval through a first database representation and

5 scoring m retrieved documents according to relevance to said query;

executing a second pass retrieval through a second database representation and scoring documents retrieved from said first pass retrieval so as to generate a final relevancy score for each document; and

wherein said second database representation comprises an $r \times m$ document matrix D, such that

 $V \approx TD$

wherein T is an $n \times r$ term matrix;

V is a non-negative n x m index matrix, wherein each of its m columns represents an j^{th} document having n entries containing the value of a function of the number of occurrences of a i^{th} term of said vocabulary appearing in said j^{th} document; and wherein T and D are non-negative matrix factors of V and r < nm/(n+m); and

wherein each of the m columns of said document matrix D corresponds to said j^{th} document.

17. The method of claim 16 wherein said final relevancy score for any jth document is a function of said jth document s corresponding entry in said document

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matrix D and the corresponding entries in said document matrix D of the Γ top-scoring documents from said first pass retrieval.

- 18. The method of claim 17 wherein said relevancy score function for said j^{th} document is proportional to a sum of cosine distances between said j^{th} document s corresponding entry in said document matrix D and each of said corresponding entries in said document matrix D of the Γ top-scoring documents from said first pass retrieval.
- 19. The method of claim 16 wherein r is at least one order of magnitude smaller than n.
- 20. The method of claim 16 wherein r is from two to three orders of magnitude smaller than n.
- 21. The method of claim 16 wherein entries of said document matrix D falling below a predetermined threshold value t are set to zero.
- 22. A program storage device readable by machine, tangibly embodying a program of instructions executable by the machine to perform method steps for information retrieval, said method steps comprising:

providing a query comprising a plurality of search terms; providing a vocabulary of *n* terms;

performing a first pass retrieval through a first database representation and scoring m retrieved documents according to relevance to said query;

executing a second pass retrieval through a second database representation and scoring documents retrieved from said first pass retrieval so as to generate a final relevancy score for each document; and

wherein said second database representation comprises an $r \times m$ document matrix D, such that

 $V \approx TD$

wherein T is an $n \times r$ term matrix;

V is a non-negative $n \times m$ index matrix, wherein each of its m columns represents an j^{th} document having n entries containing the value of a function of the number of occurrences of a i^{th} term of said vocabulary appearing in said j^{th} document; and wherein T and D are non-negative matrix factors of V and r < nm/(n+m); and

wherein each of the m columns of said document matrix D corresponds to said jth document.